## NOTATION INDEX

| Symbol | Description | Page |
| :--- | :--- | :---: |
| Aut $\mathcal{P}(\mathcal{H})$ | projective group of automorphisms of $\mathcal{P}(\mathcal{H})$ | 237 |
| $*$ | convolution of measures and functions | 125 |
| bE | bounded measurable functions on $E$ | - |
| $\mathbf{B}^{\phi}$ | bundle associated to a cocycle | 246 |
| $\mathbf{C}$ | the complex numbers | - |
| $\mathcal{C}$ | a measure class on $(X, \mathcal{X})$ | 241 |
| $\mathcal{C}_{G}$ | measure class of Haar measure on $G$ | 241 |
| $\chi$ | a channeling, $\chi \in \mathcal{I}(k)$ | 88 |
| $D(\chi)$ | domain of $\chi$ | 142 |
| $D_{q} M$ | decomposable descent of kernel $M$ by $q$ | 160 |
| $\mathcal{D}$ | linear map of measures | 194 |
| $E$ | configuration event of observer | 23 |
| $\hat{E}^{\prime} \hat{E}^{k}$ | state space of augmented dynamics | 147 |
| $\mathcal{E}$ | $\sigma$-algebra on $E$ | 23 |
| $\hat{\mathcal{E}}$ | $\sigma$-algebra on $\hat{E}$ | 147 |
| $\mathcal{E} \mathcal{E}_{+}$ | nonnegative measurable functions on $E$ | - |
| $\epsilon_{x}$ | Dirac measure on the point $x$ | - |
| $\eta$ | interpretation kernel of observer | 23 |
| $\mathcal{F}$ | $\sigma$-algebra on $\Omega$ | 109 |
| $\phi$ | a cocycle | 241 |
| $\gamma_{f}$ | group element $\gamma$ acting on function $f$ | 220 |
| $\gamma K$ | group element $\gamma$ acting on kernel $K$ | 220 |
| $\gamma_{\mu}$ | group element $\gamma$ acting on measure $\mu$ | 220 |
| $(\gamma) R$ | modification of action kernel | 223 |
| $(\gamma) A$ | modification of participator | 223 |
| $G$ | symmetry group of a symmetric framework | 93 |
| $G m$ | orbit of $m$ under group $G$ | 80 |
| $G / E$ | quotient set of $G$ by $E$ | 79 |
| $\mathcal{H}$ | Hilbert space | 231 |
| $\mathbf{H} \mathbf{H}^{1}$ | collection of all $(G, X, M)$ cohomology classes | 242 |
| $h_{*} \mu$ | "pushdown" of measure $\mu$ | 21 |
| $h^{*} f$ | "pullback" of function $f$ | 171 |
|  |  |  |


| $h^{*} \mathcal{V}$ | $\sigma$-algebra induced by $h$ | 159 |
| :---: | :---: | :---: |
| $\mathrm{Id}_{X}$ | identity map on $X$ | - |
| $\imath$ | identity element of a group | 80 |
| $\mathcal{I}(k)$ | set of involutions on subsets of $k$ elements | 142 |
| $J$ | the symmetry group of $E, J \subset G$ | 93 |
| $\hat{J}^{k}$ | $J^{k} \times \mathcal{I}(k)$ | 169 |
| $L$ | active perspectives in a channeling | 87 |
| $L^{2}(X, m)$ | (or $L^{2}(m)$ ) square integrable functions | 119 |
| $m_{p}^{\mu}$ | rcpd of $\mu$ wrt $p$, a kernel | 22 |
| $M_{\nu}(A)$ | probability measure on ( $\Omega, \mathcal{F}$ ) | 162 |
| $M_{x}(A)$ | $=M_{\nu}(A)$ with $\nu(\cdot)=\epsilon_{x}(\cdot)$ | 162 |
| N | the natural numbers | - |
| $N_{t}$ | markovian kernel, standard dynamics | 145 |
| $N_{t, \chi}$ | markovian kernel, channeling dependent | 143 |
| $N^{\dagger}$ | a kernel, $N^{\dagger}(e, A)=N(-e,-A)$ | 125 |
| $\hat{N}$ | markovian kernel, augmented dynamics | 149 |
| $\Omega$ | canonical probability space | 109 |
| $\hat{\Omega}$ | augmented chain canonical probability space | 151 |
| $\otimes$ | tensor product | - |
| $1_{A}$ | characteristic function of set $A$ | - |
| $\mathcal{P}(\mathcal{H})$ | set of orthogonal projections on $\mathcal{H}$ | 232 |
| $\mathrm{pr}_{1}$ | projection onto first factor |  |
| $P_{n}$ | $n$-fold product of kernel $P$ with itself | 109 |
| $p_{*}(\mu)$ | distribution of $p$ wrt measure $\mu$ | 21 |
| $p_{*}^{\tau}(\hat{N})$ | a kernel, the bring down of $\hat{N}$ | 154 |
| $\Pi$ | product | - |
| $\pi$ | perspective map of observer | 23 |
| $\left.\pi\right\|_{E}$ | restriction of map $\pi$ to set $E$ | - |
| $\Psi$ | quantum mechanical wave function | 233 |
| Q | the rational numbers | - |
| $Q(s, \cdot)$ | action kernel | 140 |
| $\left\langle Q_{1}, \ldots, Q_{k} \widehat{\rangle_{\tau}}\right.$ | one step T.P. for $k$ participators | 149 |
| R | the real numbers | - |
| $R_{q} M$ | respectful descent of kernel $M$ by $q$ | 158 |
| $S$ | observation event of observer | 23 |
| $\sigma$ | state of a physical system | 232 |
| $\Sigma_{m}$ | stabilizer of $m$ | 80 |
| $\mathcal{T}_{q}$ | proper time of participator $q$ | 121 |

## NOTATION

| $\tau$ | kernel for channeling probabilities | 145 |
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| $\theta(A)$ | shift operator applied to event $A$ | 109 |
| $\Theta$ | reflexive framework | - |
| $\mathcal{U}$ | group of unitary automorphisms of $\mathcal{H}$ | 237 |
| $X$ | configuration space of observer | 23 |
| $\xi$ | starting measure of participator | 140 |
| $Y$ | observation space of observer | 23 |
| $\mathbf{Z}$ | the integers | - |

